

# Beam Optics Optimization in the KEK Digital Accelerator LEBT

## Considering the Effect of Remnant Magnetic Fields

(KEK-DA LEBT 残留磁場影響におけるイオンビームオプティックス最適化)

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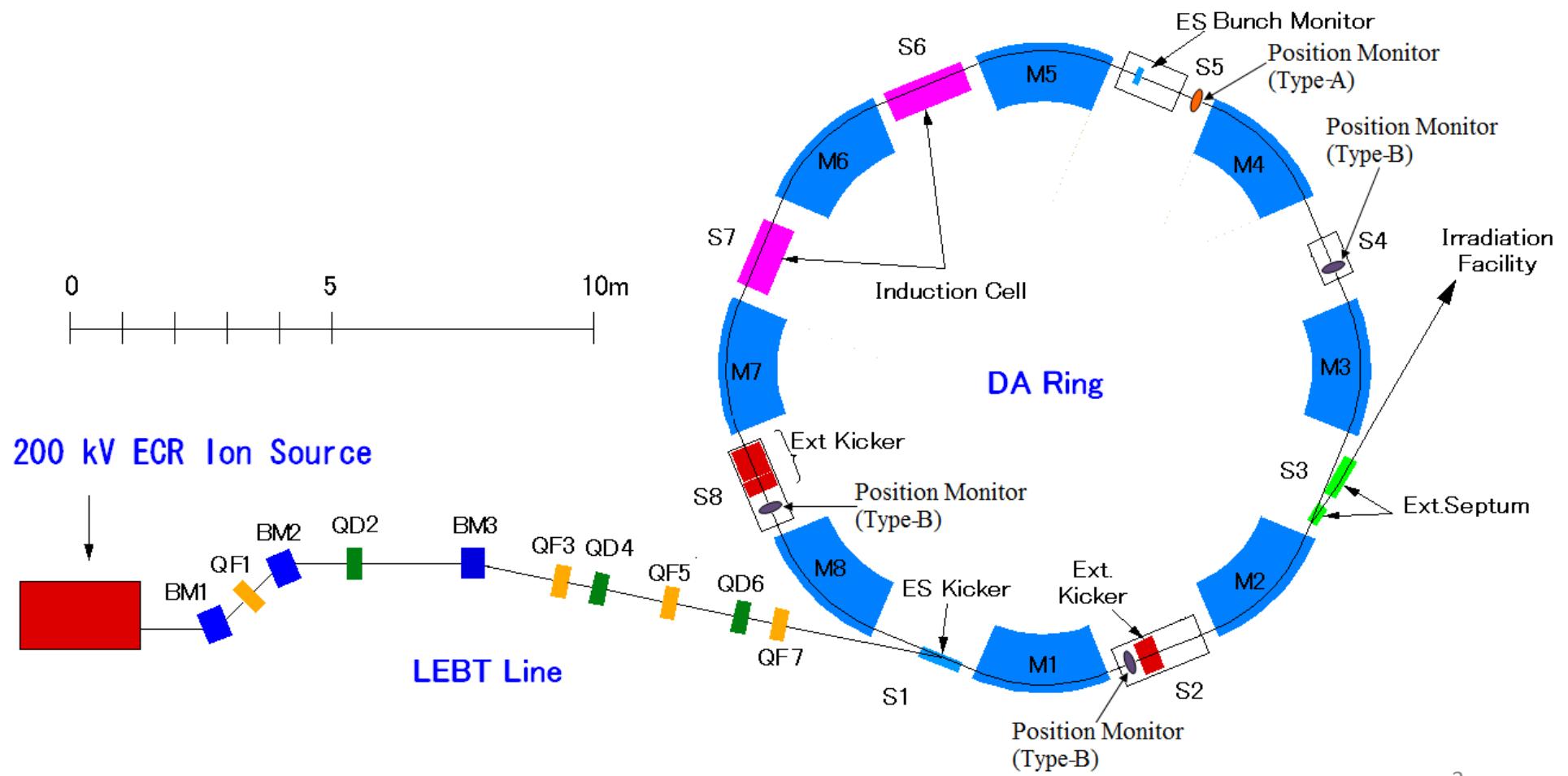
# SYLLABUS

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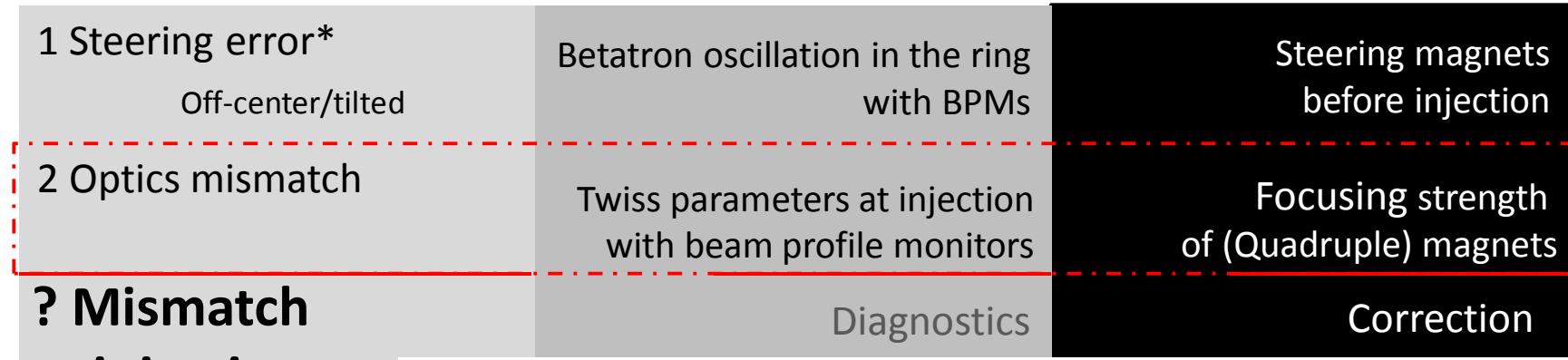
- About KEK Digital Accelerator
- Motivation
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- Data Analysis Results
- Discussion
- Summary and Future work

# About KEK Digital Accelerator

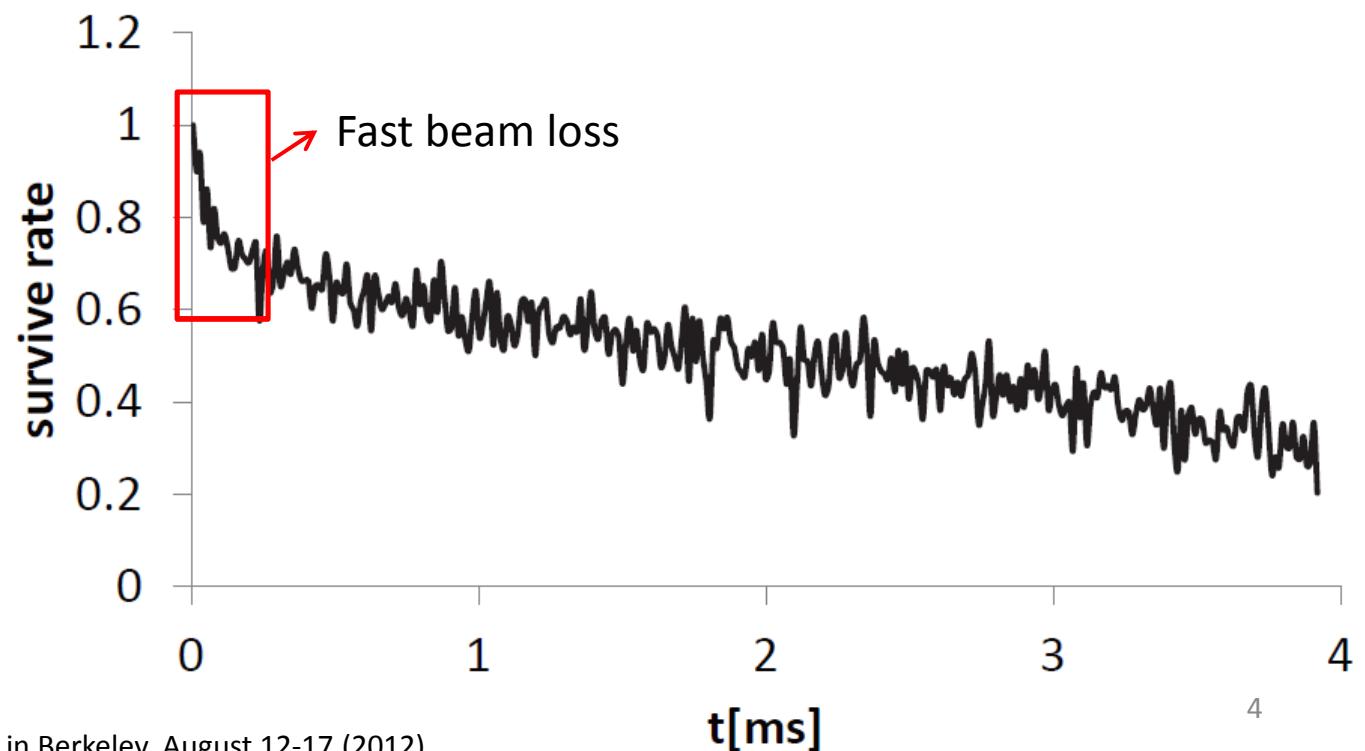
- [1] K.Takayama, and J.Kishiro, *Nucl. Inst. Meth. Phys. Res. A* 451, 304 (2000).  
[2] T. Iwashita et al., *Phys. Rev. ST-AB* **14**, 071301 (2011).



# Motivation



Beam emittance blow up  
Beam size increasing  
Beam loss



\*T.Yoshimoto et al., in Proc. of HIF2013 in Berkeley, August 12-17 (2012).

# Theoretical Background

the magnetic settings  
(excitation currents)

$$\downarrow \\ m_{11}, m_{12}, m_{13}$$

$$\downarrow \\ \varepsilon\beta_1$$

$$\boxed{[\varepsilon\beta_1]^i = m_{11}^i\varepsilon\beta_0 + m_{12}^i\varepsilon\alpha_0 + m_{13}^i\varepsilon\gamma_0 \\ i = 1, 2, 3, 4, 5, \dots, n}$$

*ε – emittance*

$$\varepsilon\beta_1 = m_{11}\varepsilon\beta_0 + m_{12}\varepsilon\alpha_0 + m_{13}\varepsilon\gamma_0$$

fitting for  $(\varepsilon\beta_0, \varepsilon\alpha_0, \varepsilon\gamma_0)$

$$\varepsilon = \sqrt{\varepsilon\beta_0\varepsilon\gamma_0 - \varepsilon\alpha_0}$$

and

$$\beta_0, \alpha_0, \gamma_0$$

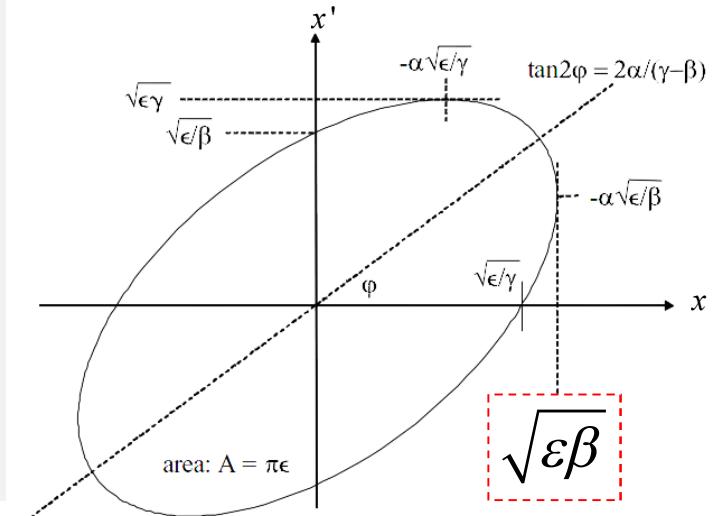
with specific setting  
transfer these for  $(\beta_1, \alpha_1, \gamma_1)$

Compare with ring lattice  
for mismatch estimation

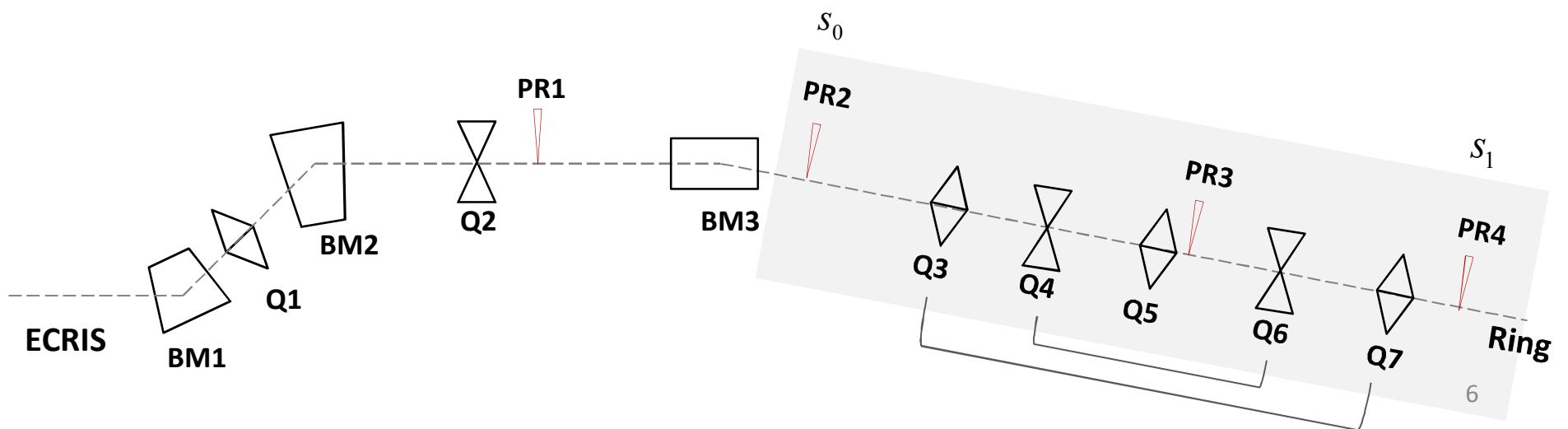
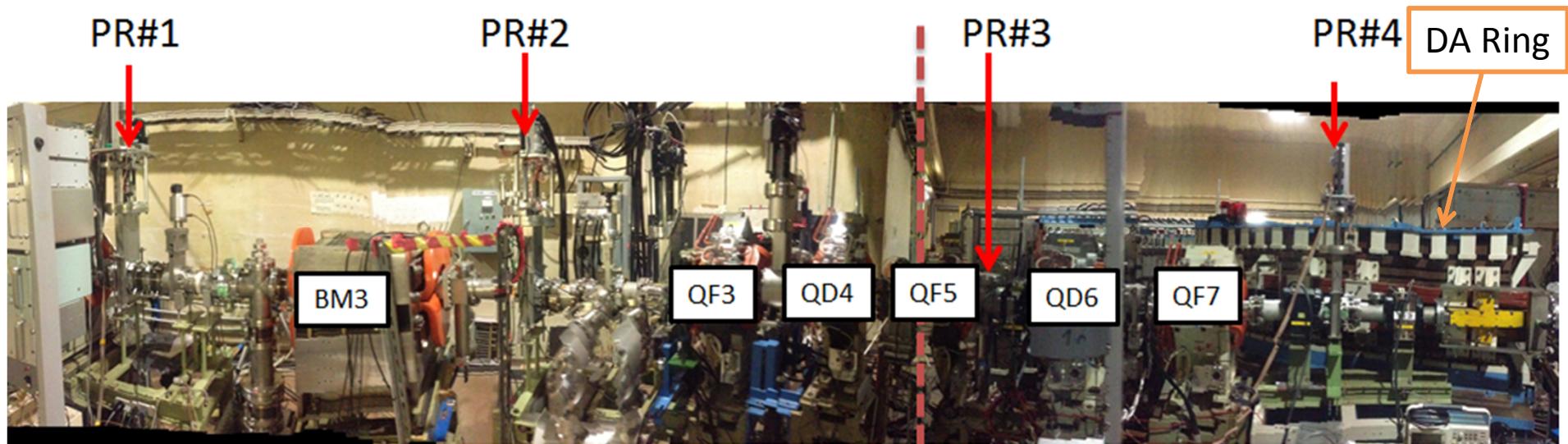
from  $s_0$  to  $s_1$ ,

$$\begin{pmatrix} \beta_1 \\ \alpha_1 \\ \gamma_1 \end{pmatrix} = \begin{pmatrix} m_{11} & m_{12} & m_{13} \\ m_{21} & m_{22} & m_{23} \\ m_{31} & m_{32} & m_{33} \end{pmatrix} \begin{pmatrix} \beta_0 \\ \alpha_0 \\ \gamma_0 \end{pmatrix}$$

$$\begin{pmatrix} \varepsilon\beta_1 \\ \varepsilon\alpha_1 \\ \varepsilon\gamma_1 \end{pmatrix} = \begin{pmatrix} m_{11} & m_{12} & m_{13} \\ m_{21} & m_{22} & m_{23} \\ m_{31} & m_{32} & m_{33} \end{pmatrix} \begin{pmatrix} \varepsilon\beta_0 \\ \varepsilon\alpha_0 \\ \varepsilon\gamma_0 \end{pmatrix}$$



# LEBT and Wire Monitors



# Quadruples and their remnant parts

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Focusing Plane

$$\begin{pmatrix} \cos[l\sqrt{k}] & \frac{1}{\sqrt{k}} \sin[l\sqrt{k}] \\ -\sqrt{k} \sin[l\sqrt{k}] & \cos[l\sqrt{k}] \end{pmatrix}$$

$$k = \frac{B'}{B\rho}$$

Magnetic rigidity

Defocusing Plane

$$\begin{pmatrix} \cosh[l\sqrt{k}] & \frac{1}{\sqrt{k}} \sinh[l\sqrt{k}] \\ \sqrt{k} \sinh[l\sqrt{k}] & \cosh[l\sqrt{k}] \end{pmatrix}$$

$$\mathbf{B}' = \mathbf{g} \times \mathbf{I}[A] + \mathbf{b}$$

Remnant part

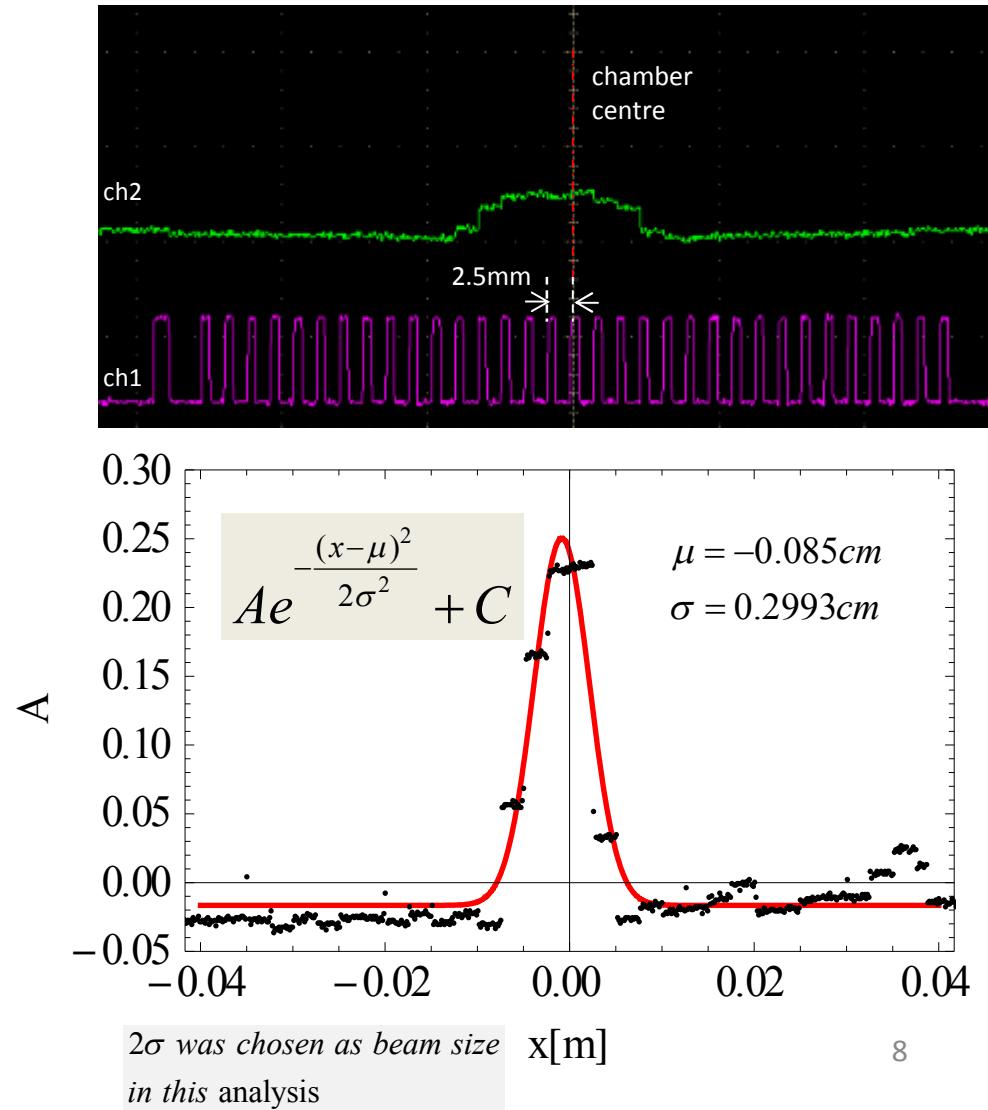
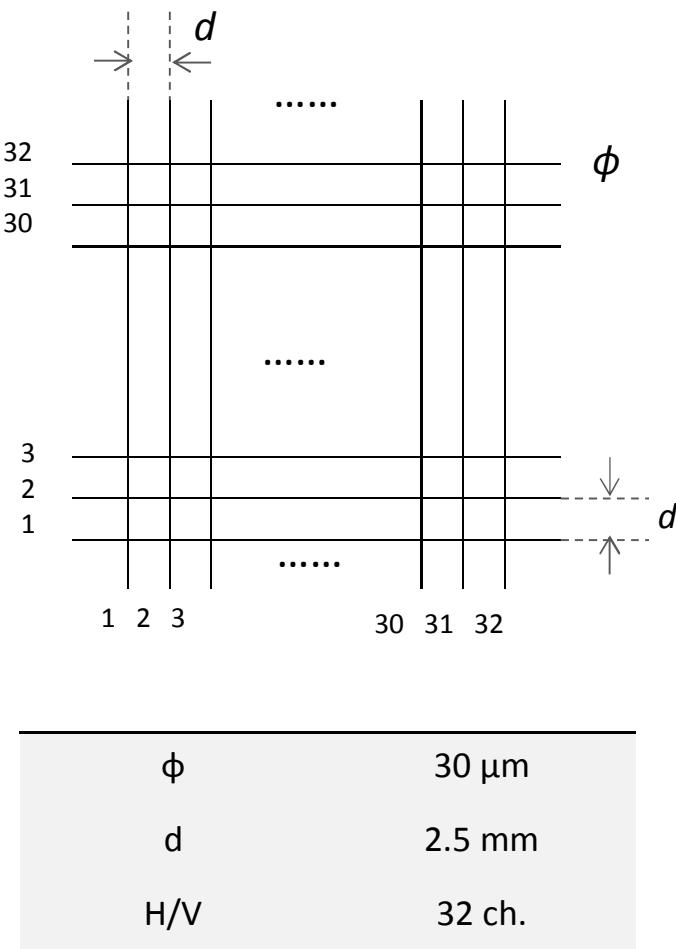
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g	b
0.0408	0.0207

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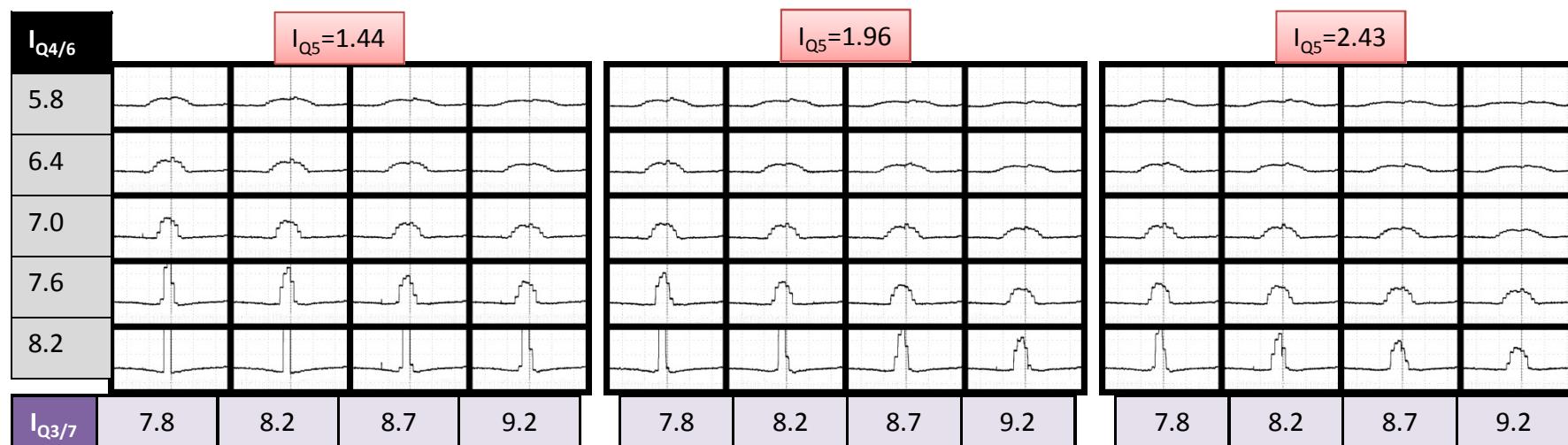
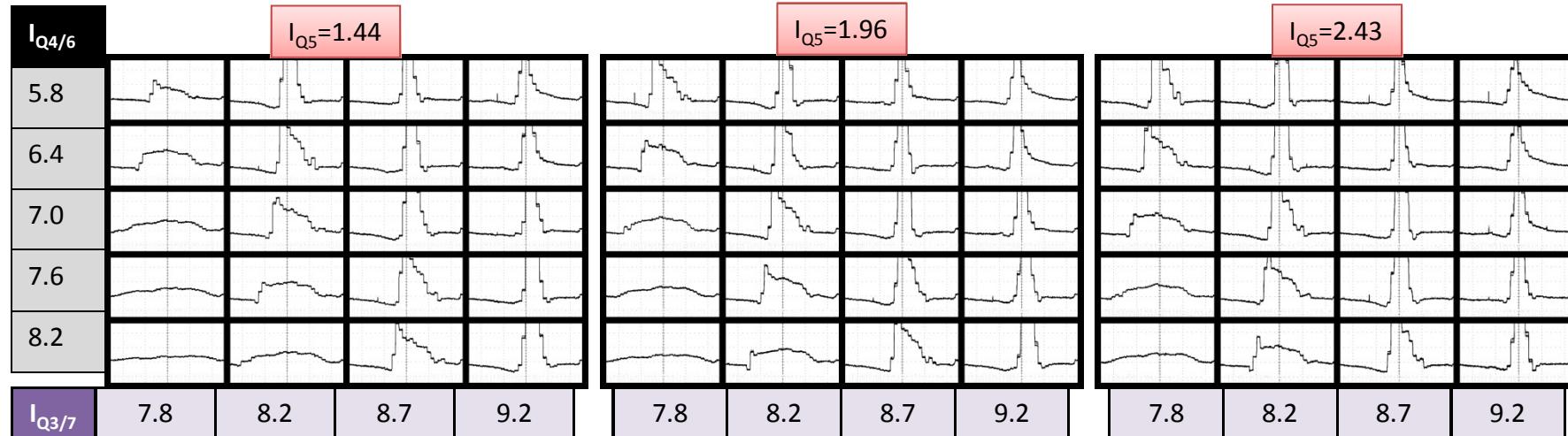
\* KEK DA Note 08-92 (*internal report*).

# Wire Monitor and its signal



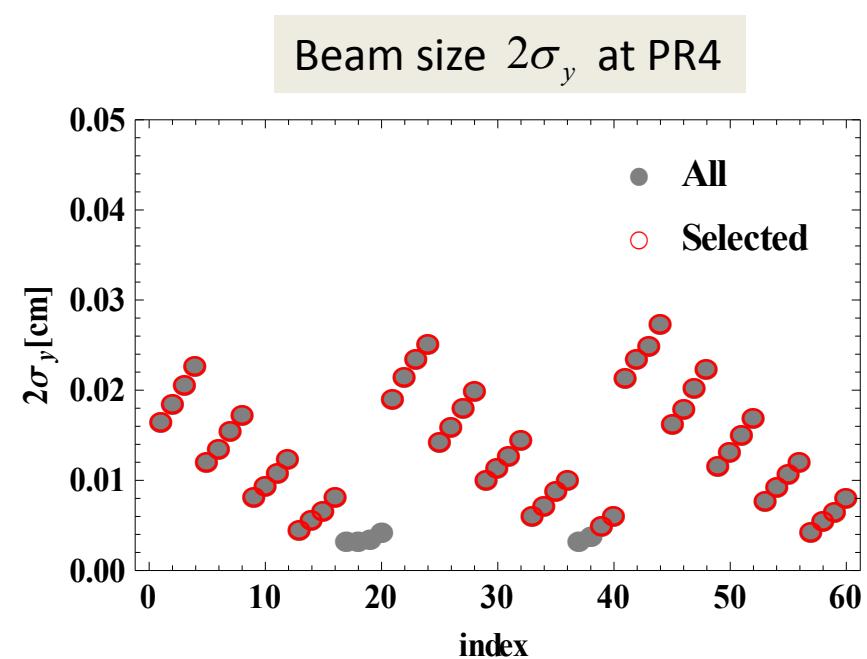
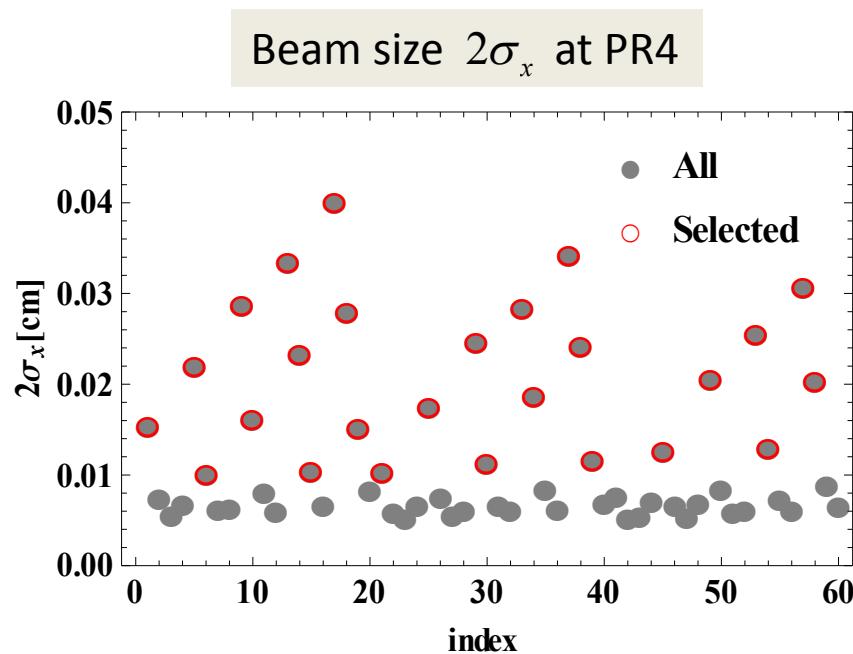
# Experimental Observation(PR4)

excitation currents  $\rightarrow m_{11}, m_{12}, m_{13} \rightarrow \varepsilon\beta_1(\text{beam size})$



# Data Selection and Constraints

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## Constraints

Beam size at PR2:

$$2\sigma_x = \sqrt{\varepsilon_x \beta_{x0}} = 1.2 \text{ cm}$$

$$2\sigma_y = \sqrt{\varepsilon_y \beta_{y0}} = 0.6 \text{ cm}$$

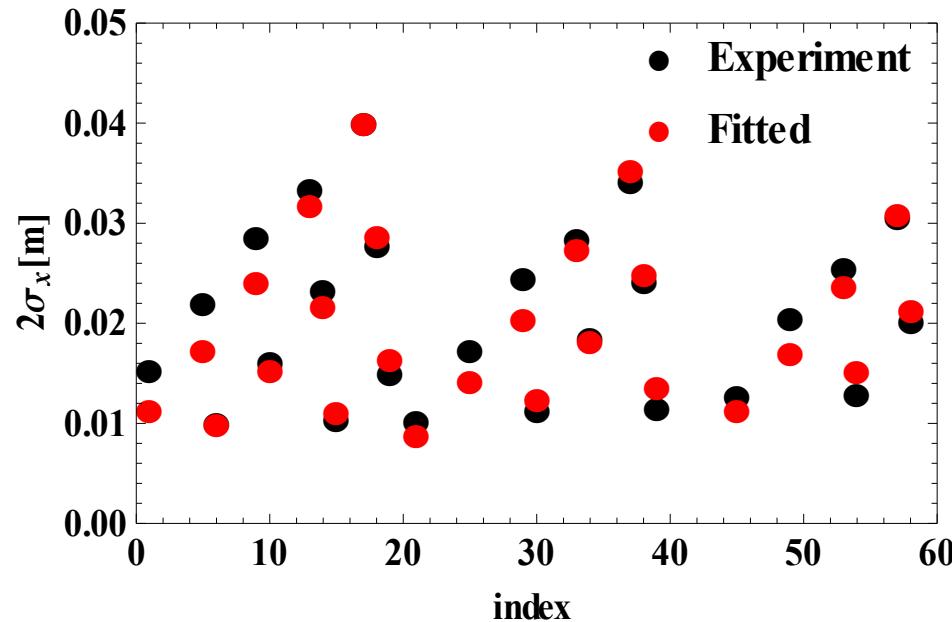
Beam emittance

$$\varepsilon = \sqrt{\varepsilon \beta_0 \varepsilon \gamma_0 - \varepsilon \alpha_0} > 0$$

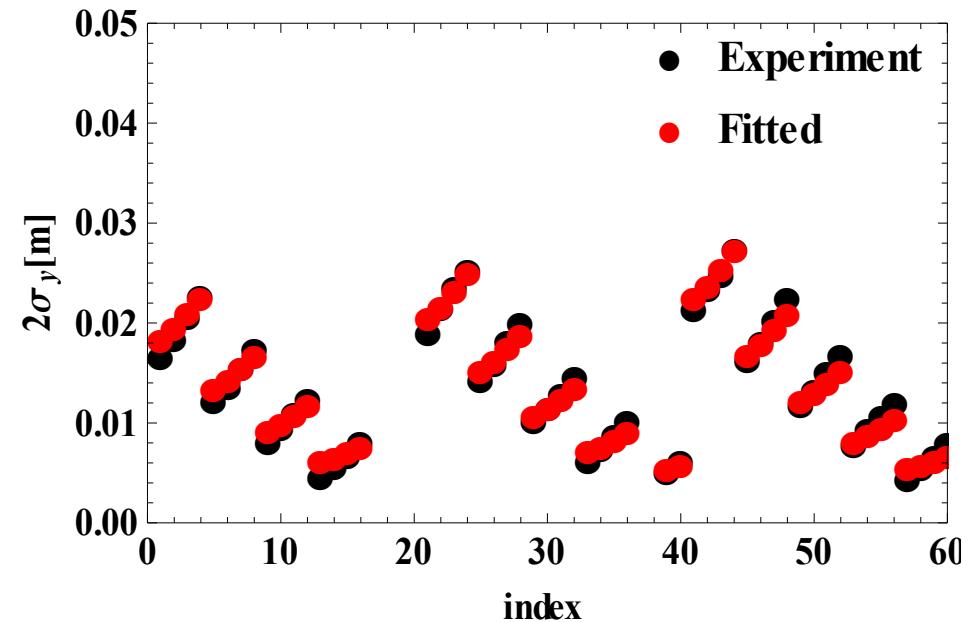
# Fitting Results

With remnant part all be 0.0207

Horizontal



Vertical

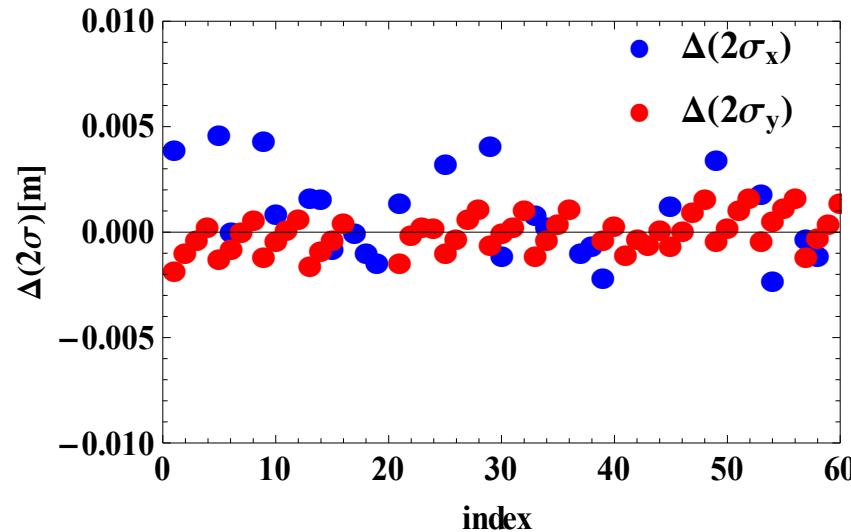


$\beta_{x0}$ [m]	$\alpha_{x0}$	$\gamma_{x0}$	$\varepsilon_x$ [ $\mu\text{m} \cdot \text{rad}$ ]	$2\sigma_{x0}$
3.32	-3.51	4.02	44.98	1.22

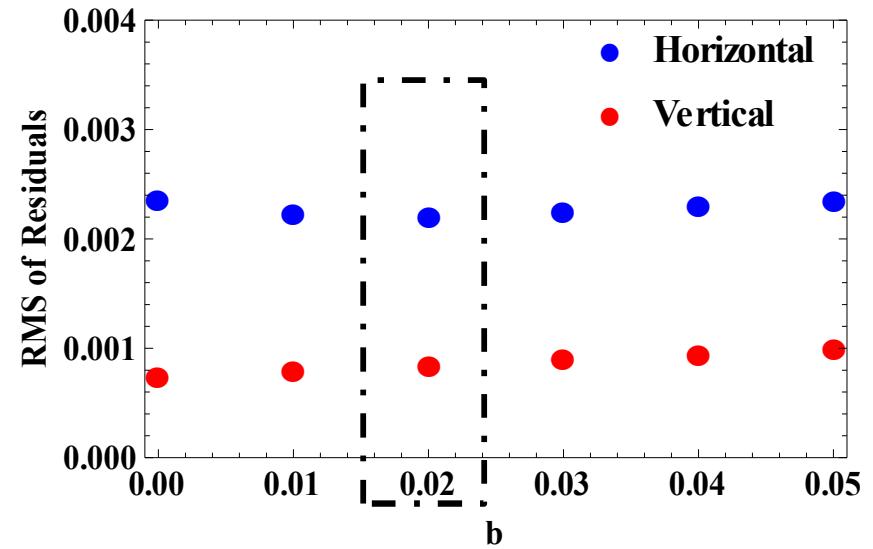
$\beta_{y0}$ [m]	$\alpha_{y0}$	$\gamma_{y0}$	$\varepsilon_y$ [ $\mu\text{m} \cdot \text{rad}$ ]	$2\sigma_{y0}$
2.48	1.44	.24	24.78	0.78

# Remnant Part

Fitting Residuals



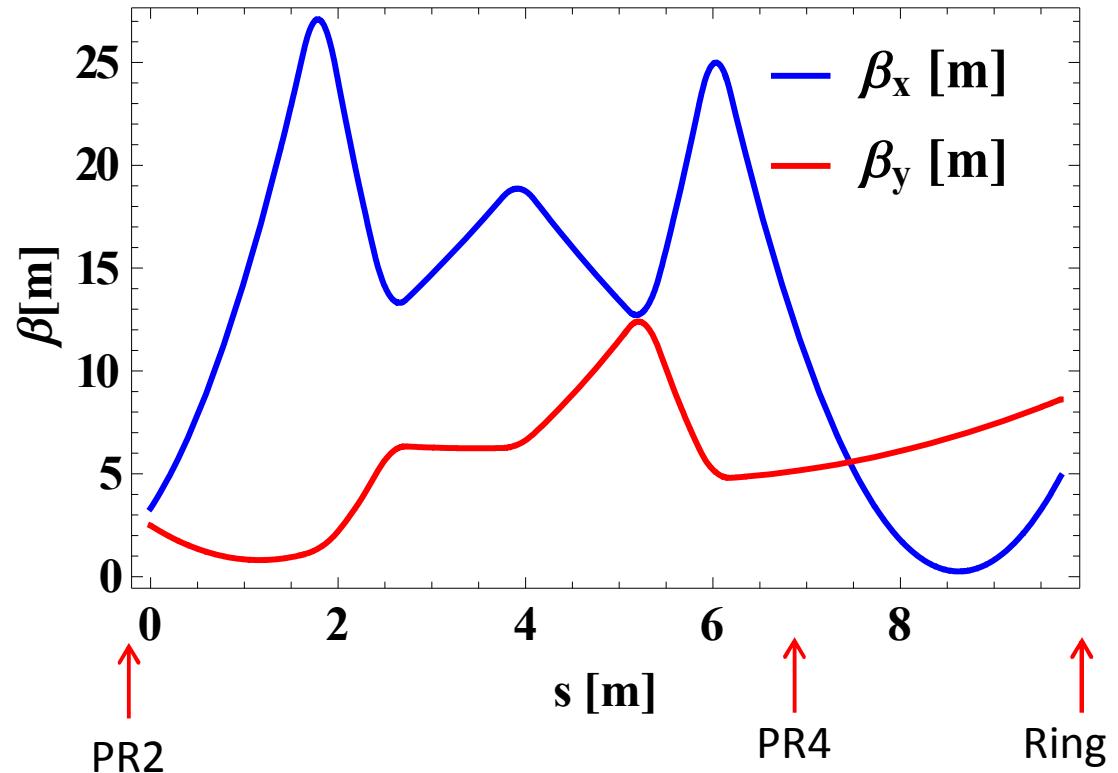
RMS of Residuals



$$B' = g \cdot I[A] + \mathbf{b}$$

- #1 The residuals follow the same pattern as data points
- #2 With all remnant parts the same, present choice is a good one

# Beta Function



LEBT Lattice	$\beta_{xi}$	$\alpha_{xi}$	$\gamma_{xi}$	$\beta_{xr}$	$\alpha_{xr}$	$\gamma_{xr}$
	4.89	-4.26	3.92			
	$\beta_{yi}$	$\alpha_{yi}$	$\gamma_{yi}$	$\beta_{xr}$	$\alpha_{xr}$	$\gamma_{xr}$
	8.62	-0.92	0.21	1.90	0.48	0.65

Ring Lattice

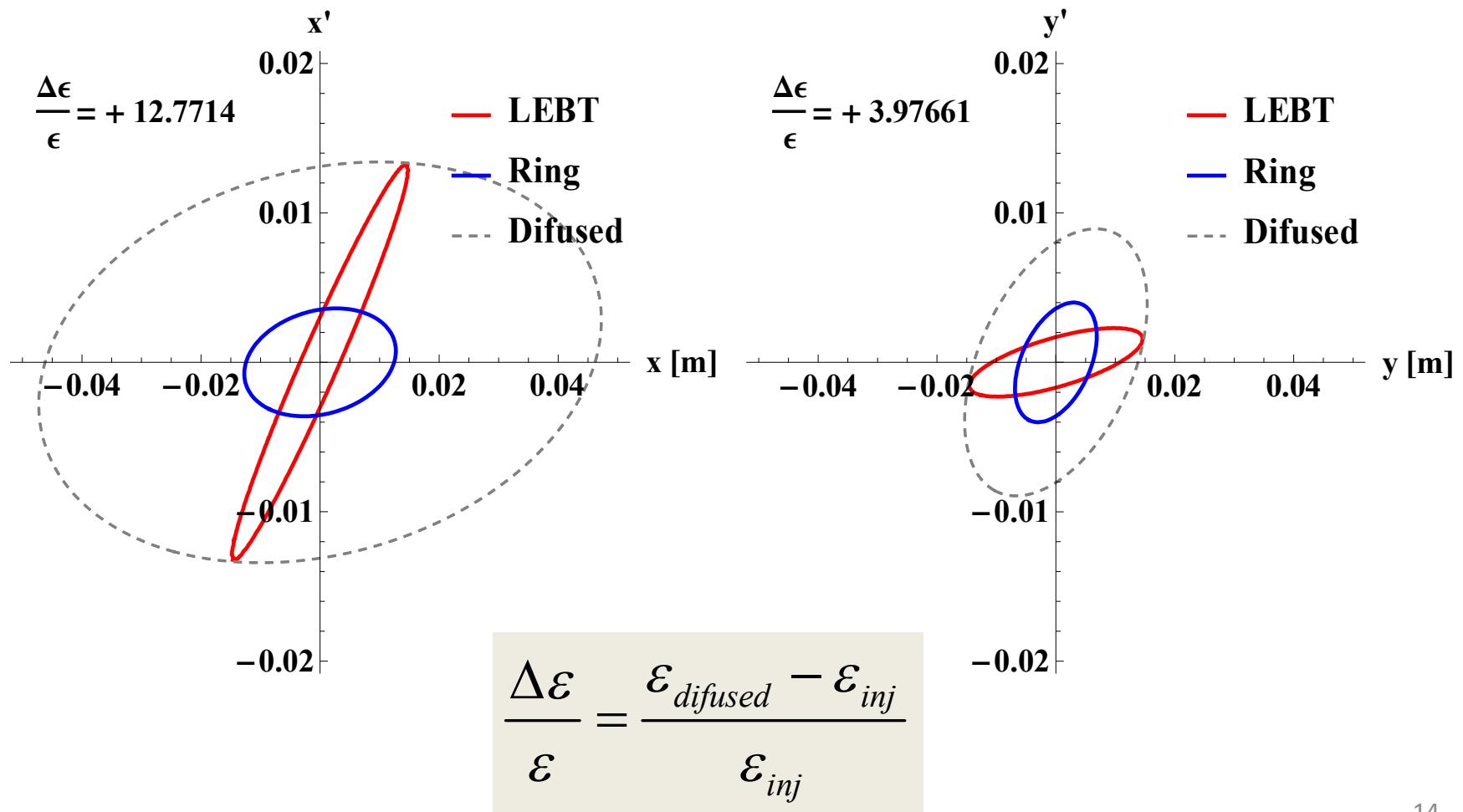
Excitation Current(A)		
$I_{Q3/Q7}$	7.5	
$I_{Q4/Q6}$	7.0	
$I_{Q5}$	2.3	

Beam size(cm)		
$x_{\max}$	3.5	
$y_{\max}$	1.8	
$x_{\min}$	0.7	
$y_{\min}$	0.5	

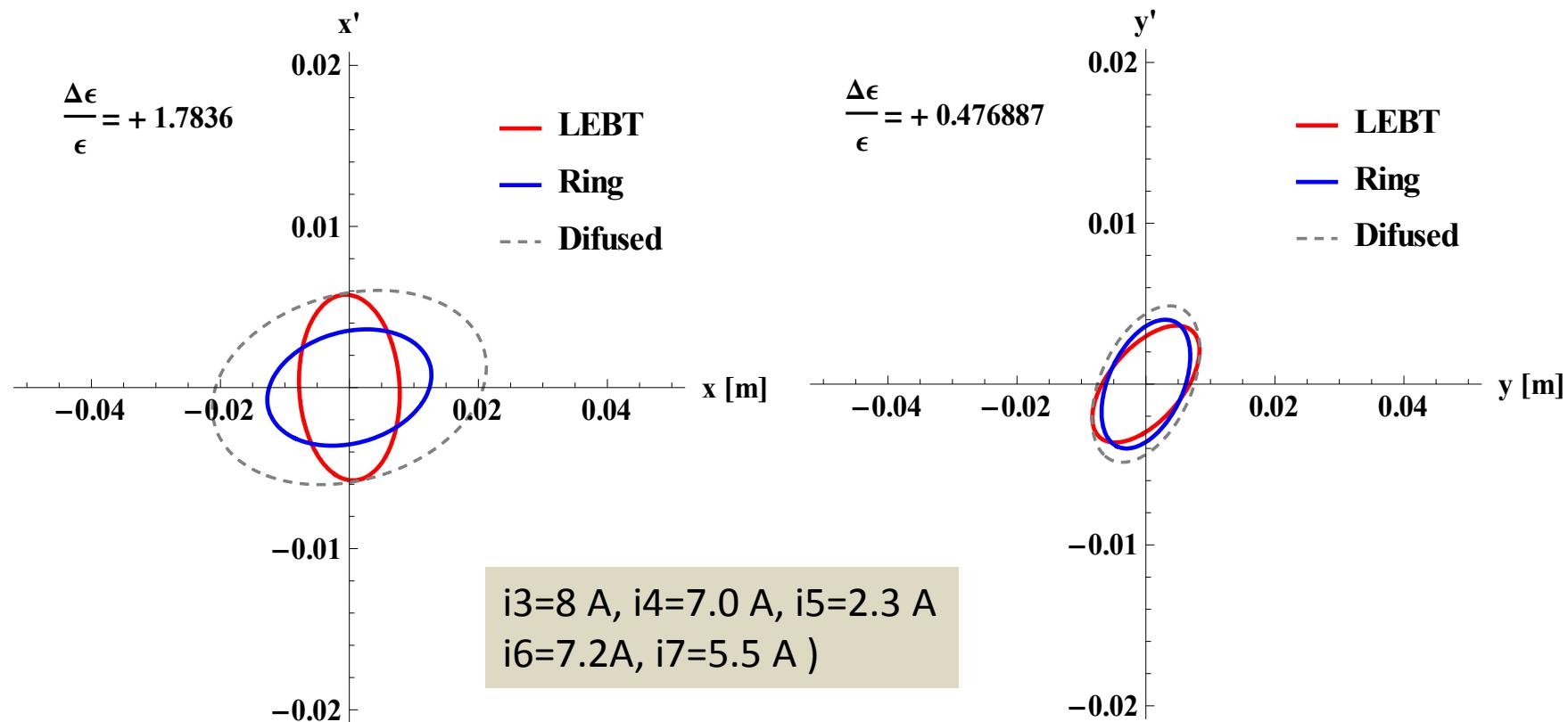
# Injection Mismatch

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# Possible Solutions

## #1 Independent excitation currents



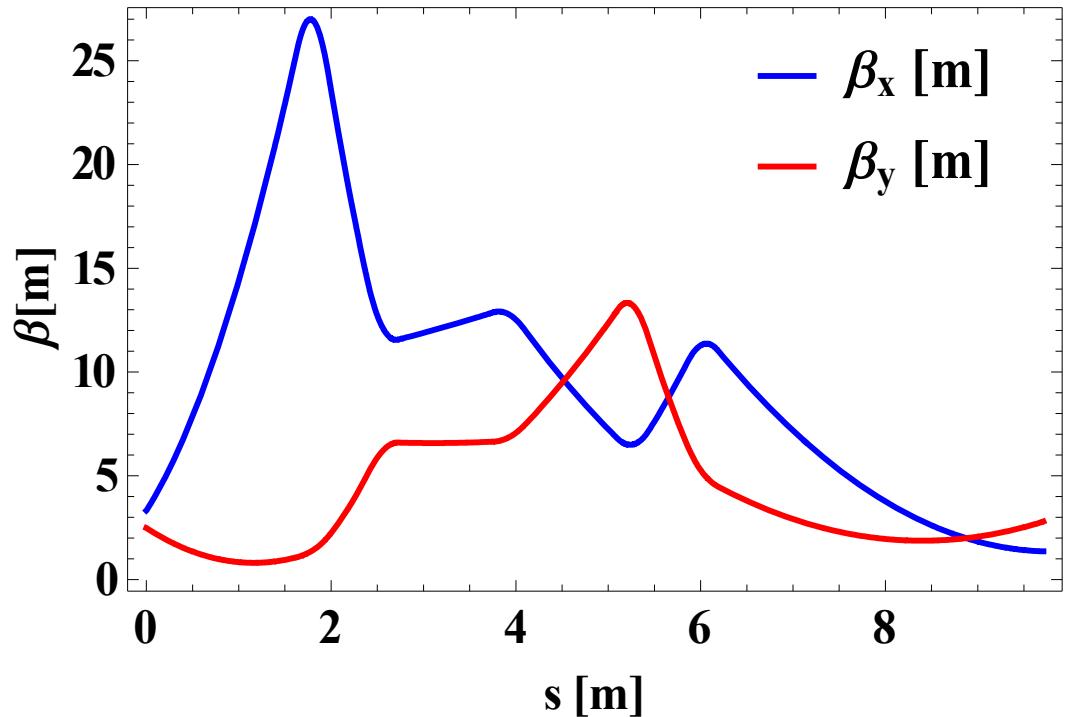
## #2 Upstream optimization

# Summary and Future Works

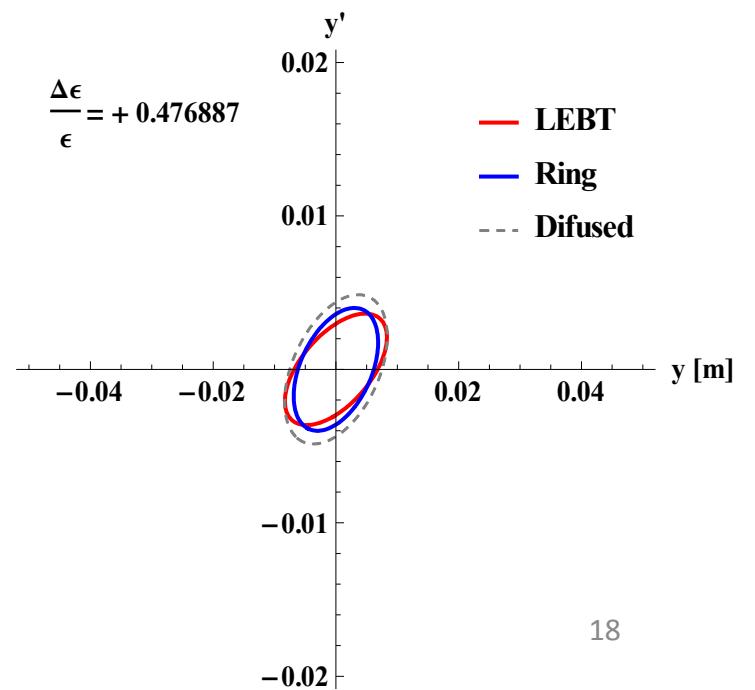
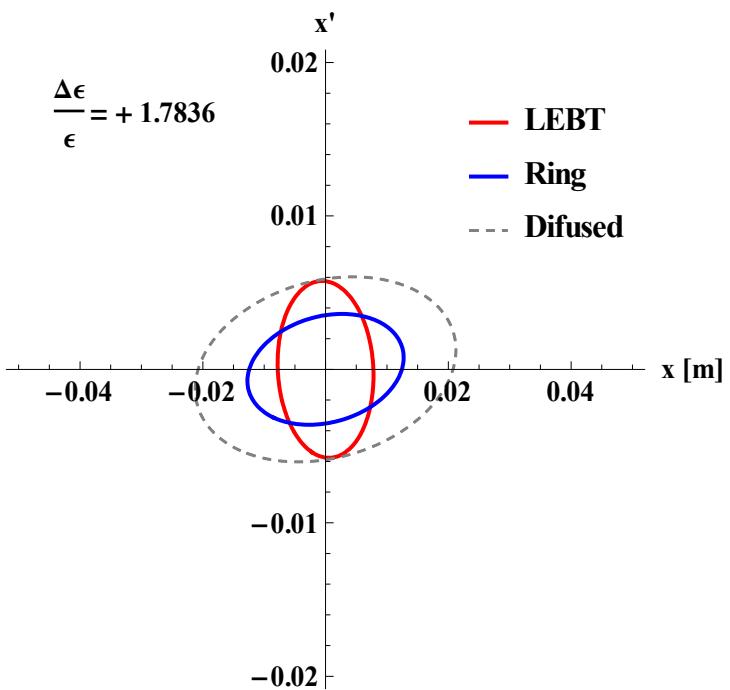
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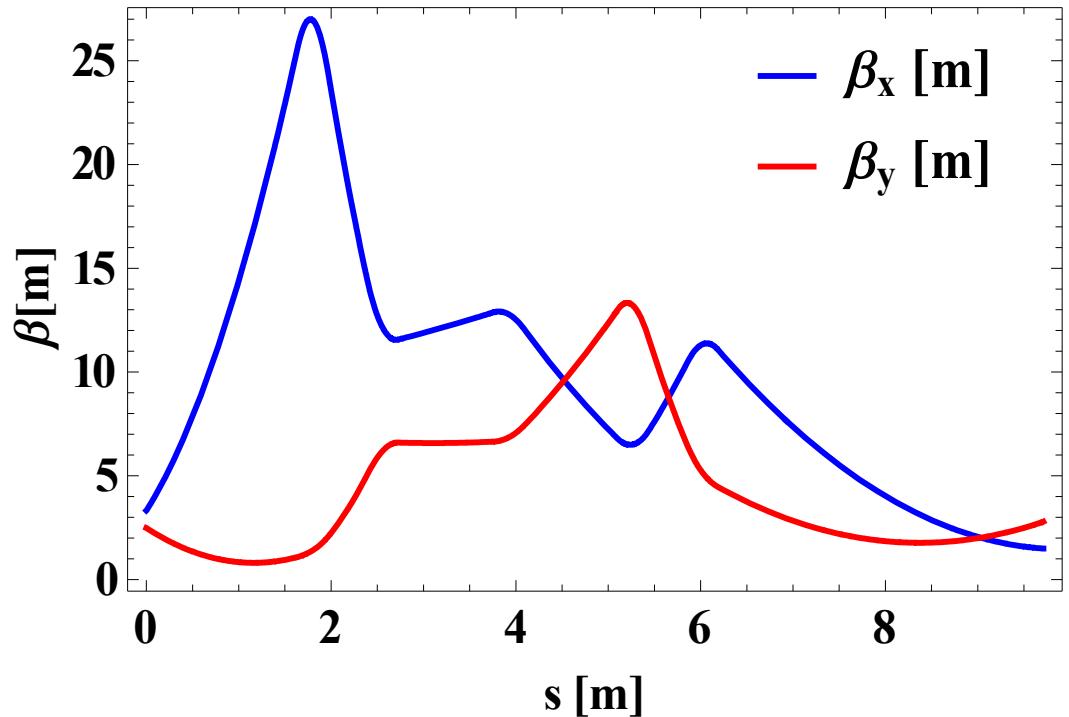
- ✓ With the help of wire monitors, the Twiss parameters and emittance in LEBT region could be determined experimentally
- ✓ Consequently, the optics focusing mismatch could be estimated
- ✓ Experiments aiming at the two possible solutions are planned after summer shutdown and hopefully we can reduce the fast beam loss at the beginning of commissioning

# THANKS



$$\begin{aligned} & \{iQ3, iQ4, iQ5, iQ6, iQ7\} \\ & = \{8., 7.2, 3.7, 2.7, \textcolor{red}{5.5}\} \end{aligned}$$





$$\begin{aligned} & \{iQ3, iQ4, iQ5, iQ6, iQ7\} \\ & = \{8., 7, 2.3, 7.2, \textcolor{red}{5.4}\} \end{aligned}$$

